

①

p	q	$p \oplus q$	$p \vee (p \oplus q)$	$(p \vee (p \oplus q)) \wedge q$
0	0	0	0	0
0	1	1	1	1
1	0	1	1	0
1	1	0	1	1

Identical

$$(p \vee (p \oplus q)) \wedge q \iff q$$

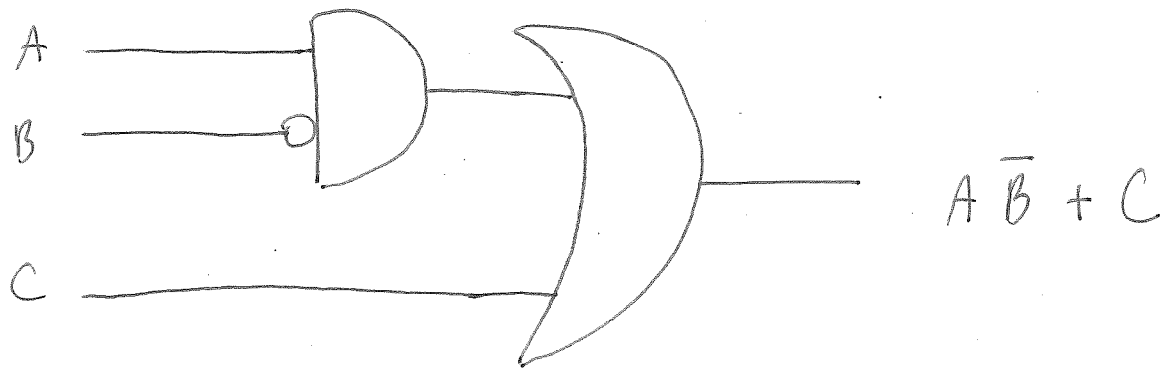
②

p	q	$p \vee q$	$\sim p$	$\sim p \wedge (p \vee q)$	$\sim p \wedge q$
0	0	0	1	0	0
0	1	1	1	1	1
1	0	1	0	0	0
1	1	1	0	0	0

Identical

Yes

③



④ a) $r \wedge (\sim p \vee q) \Leftrightarrow (r \wedge \sim p) \vee (r \wedge q)$
Distributive

b) $AB(\bar{A}\bar{B} + C) = ABC$ Absorption

c) $\overline{\bar{C}D} = \bar{C} + \bar{D}$ De Morgan's

⑤ $\sim((p \vee \sim q) \wedge \sim p)$

$\Leftrightarrow \sim(p \vee \sim q) \vee \sim(\sim p)$ De Morgan's

$\Leftrightarrow \sim p \wedge \sim(\sim q) \vee \sim(\sim p)$ De Morgan's

$\Leftrightarrow \sim p \wedge q \vee p$ Complement (twice)

$\Leftrightarrow p \vee (\sim p \wedge q)$ Commutative

$\Leftrightarrow p$ Absorption

⑥ If $\underbrace{x \text{ equals } 3}_p$ then $\underbrace{y \text{ does not equal } 7}_q$.

a) The inverse is $\sim p \rightarrow \sim q$

If x does not equal 3 then y equals 7.
Not logically equivalent to $p \rightarrow q$.

b) The converse is $q \rightarrow p$
If y does not equal 7 then x equals 3.
Not logically equivalent to $p \rightarrow q$.

c) The contrapositive is $\sim q \rightarrow \sim p$
If y equals 7 then x does not equal 3.
This IS logically equivalent to $p \rightarrow q$.

⑦ a) No

b) YES

c) YES

d) No