

1. [2 marks] A company car is valued at $y = 62,500 - 2370x$, where y is in dollars and x is the number of years after 2019.

a) In which year will the value be \$22,210?

$$\begin{aligned} \text{Sub } y = 22210: \quad & 22210 = 62500 - 2370x \\ & -40290 = -2370x \\ & 17 = x \end{aligned}$$

$$\begin{aligned} x &= \text{year} - 2019 \\ 17 &= \text{year} - 2019 \\ 2036 &= \text{year} \end{aligned}$$

b) What was the value in the year 2025?

$$\begin{aligned} x &= \text{year} - 2019 \\ x &= 2025 - 2019 \\ x &= 6 \end{aligned}$$

$$\begin{aligned} \text{Sub } x = 6: \quad & y = 62500 - 2370(6) \\ & y = \$48,280 \end{aligned}$$

2. [2 marks] At a certain company: 32% of employees are gym members, 40% of employees work in finance, and 18% of employees work in finance and are gym members. Find the probability that an employee who works in finance is a gym member. given

$$\begin{aligned} & \text{Pr}(\text{gym member} \mid \text{finance}) \\ &= \frac{\text{Pr}(\text{gym member and finance})}{\text{Pr}(\text{finance})} \\ &= \frac{0.18}{0.4} \\ &= 0.45 \end{aligned}$$

3. [2 marks] Events E and F are independent.
Calculate $Pr(E)$ in each situation.

a) $Pr(E \cap F) = 0.56$ and $Pr(F) = 0.7$

$$Pr(E \cap F) = Pr(E) \cdot Pr(F) \text{ if } E \text{ and } F \text{ are independent.}$$
$$0.56 = Pr(E) (0.7)$$
$$0.8 = Pr(E)$$

b) $Pr(E|F) = 0.3$ and $Pr(F) = 0.4$

$$Pr(E|F) = Pr(E) \text{ if } E \text{ and } F \text{ are independent.}$$
$$0.3 = Pr(E)$$

4. [3 marks] Four radio stations each randomly select one of 12 broadcast frequencies. What is the probability that at least two of the stations select the same frequency?

E: at least 2 stations select the same frequency
E': all stations select different frequencies

$$n(S) = 12 \times 12 \times 12 \times 12 = 12^4$$

$$n(E') = P(12, 4) \text{ or } 12 \times 11 \times 10 \times 9 = 11880$$

$$Pr(E') = \frac{11880}{12^4} \approx 0.57$$

$$Pr(E) = 1 - Pr(E') \approx 0.43$$

5. [3 marks] A box contains nine \$20 bills and seven \$100 bills. You pay \$30 and randomly draw a bill from the box. Let X be your net winnings (in dollars).

a) Find the probability distribution of X .

$$X = \text{net winnings } (\$)$$

$$= \text{amount won} - 30$$

| | |
|------------|-------|
| \$20 | \$100 |
| 9 | 7 |
| total = 16 | |

| | X | $P(X)$ |
|-------------------|-----|--------|
| draw a \$20 bill | -10 | 9/16 |
| draw a \$100 bill | 70 | 7/16 |

b) Find the expected value of X .

$$\mu = -10 \left(\frac{9}{16} \right) + 70 \left(\frac{7}{16} \right)$$

$$\mu = 25$$

$$\text{or } E(X) = 25$$

We expect to win \$25 net, on average.

6. [4 marks] A telemarketer has a 12% chance of making a sale on each call. Find the probability that the telemarketer makes a sale on at most two of the next 20 calls.

Binomial Experiment

$$n = 20$$

$$p = 0.12$$

$$q = 1 - p = 0.88$$

x = # of sales made

$$P(x \leq 2)$$

$$= P(x=0) + P(x=1) + P(x=2)$$

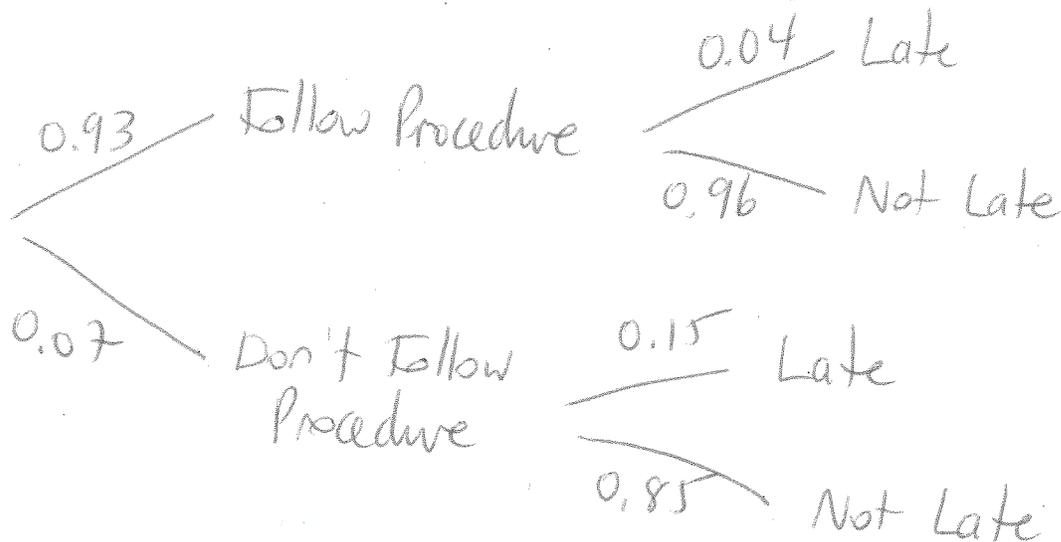
$$\boxed{\binom{n}{x} p^x q^{n-x}}$$

$$= \binom{20}{0} (0.12)^0 (0.88)^{20} + \binom{20}{1} (0.12)^1 (0.88)^{19} \\ + \binom{20}{2} (0.12)^2 (0.88)^{18}$$

$$\approx 0.56$$

7. [4 marks] Employees at a courier company follow procedure 93% of the time. When procedure is followed, 4% of packages are delivered late. When procedure is not followed, 15% of packages are delivered late. What is the probability that procedure was followed, given that a package is delivered late?

given



$$\begin{aligned}
 & \Pr(\text{Follow Procedure} \mid \text{Late}) \\
 &= \frac{\Pr(\text{Follow Procedure} \cap \text{Late})}{\Pr(\text{Late})} \\
 &= \frac{0.93(0.04)}{[0.93(0.04) + 0.07(0.15)]} \\
 &\approx 0.78
 \end{aligned}$$