

Do Suggested HW for Section 1.1  
Suggested HW and answers on website  
[www.leahhoward.com](http://www.leahhoward.com)

## 1.1 Decimal and Octal Ent'd

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Octal: Base 8

Allowed digits: 0, 1, 2, ..., 7

Decimal	Octal
0	$0_8$
1	$1_8$
2	$2_8$
3	$3_8$
⋮	
7	$7_8$
8	$10_8$
9	$11_8$
10	$12_8$
⋮	
63	$77_8$
64	$100_8$
65	$101_8$

Consider

$645_8$

64 place ( $8^2$ )      8 place ( $8^1$ )      5 place ( $8^0=1$ )

Ex: Convert to decimal

$$\text{a) } 5604_8 = 5 \times 8^3 + 6 \times 8^2 + 0 \times 8^1 + 4 \times 8^0$$

$\begin{array}{cccc} \uparrow & \uparrow & \uparrow & \uparrow \\ 8^3 \text{ place} & & & 1 \text{ place} \end{array}$

$$= 5 \times 512 + 6 \times 64 + 4 \times 1$$
$$= 2948$$

$$\text{b) } 212_3 = 2 \times 9 + 1 \times 3 + 2 \times 1$$

$\begin{array}{ccc} \uparrow & \uparrow & \uparrow \\ 9 \text{ place} & 3 \text{ place} & 1 \text{ place} \end{array}$

$$= 23$$

What's wrong with writing  $218_3$  ?  
8 is not an allowed digit.

## 1.2 Binary and Hexadecimal

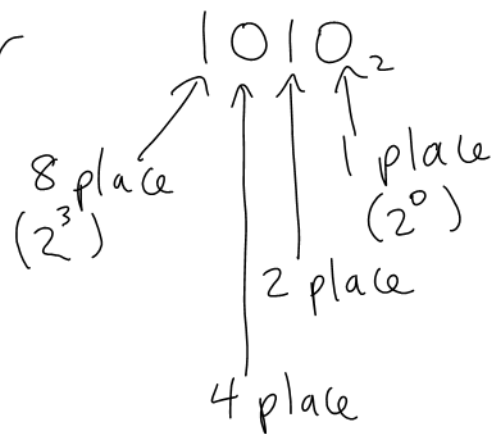
Binary: Base 2

Allowed digits: 0, 1

These are called "bits" or "binary digits"

Decimal	Binary
1	$1_2$
2	$10_2$
3	$11_2$
4	$100_2$
5	$101_2$

Consider



Ex: Convert to decimal

$$a) \quad 1100_2 = 1 \times 2^3 + 1 \times 2^2$$

$\begin{matrix} \uparrow \uparrow \uparrow \uparrow \\ 2^3 \quad \quad 2^0 \\ \text{place} \end{matrix}$

$$= 12$$

$$b) \quad 101110_2 = 1 \times 2^5 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1$$

$\begin{matrix} \uparrow \quad \quad \quad \uparrow \\ 2^5 \quad \quad \quad 2^0 \\ \text{place} \end{matrix}$

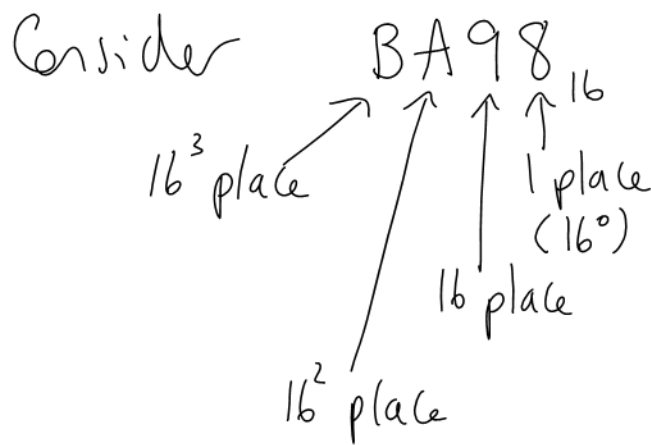
$$= 32 + 8 + 4 + 2$$

$$= 46$$

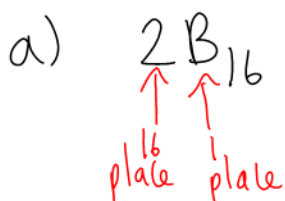
Hexadecimal: Base 16

Allowed digits: 0, 1, ..., 9, A, B, C, D, E, F

Decimal	Hexadecimal
0	0 <sub>16</sub>
⋮	⋮
9	9 <sub>16</sub>
10	A <sub>16</sub>
11	B <sub>16</sub>
12	C <sub>16</sub>
13	D <sub>16</sub>
14	E <sub>16</sub>
15	F <sub>16</sub>
16	10 <sub>16</sub>
17	11 <sub>16</sub>



Ex: Convert to decimal



Hex.	Decimal
9 <sub>16</sub>	9
A <sub>16</sub>	10
B <sub>16</sub>	11
C <sub>16</sub>	12
⋮	⋮

$$= 2 \times 16 + \underline{\underline{B}} \times 1$$

$$= 43$$

$$\begin{aligned} \text{b) } 98003_{16} &= 9 \times 16^4 + 8 \times 16^3 + 3 \times 1 \\ &\quad \begin{array}{l} \uparrow \\ 16^4 \text{ place} \end{array} \quad \begin{array}{l} \uparrow \\ 1 \text{ place} \end{array} \\ &= 622\ 595 \end{aligned}$$

$$\begin{aligned} \text{c) } B055_{16} &= \underline{\underline{B}} \times 16^3 + 5 \times 16 + 5 \times 1 \\ &\quad \begin{array}{l} \uparrow \\ 16^3 \text{ place} \end{array} \\ &= 45\ 141 \end{aligned}$$

$9_{16} = 9$
$A_{16} = 10$
$B_{16} = 11$