

Test 1

Fri Sept 29

Bring calculator.

Bring music / earplugs.

Practice Problems on website.

Covers

1.2-1.5 Limits

2.2-2.4 Polynomial / Trig Derivatives

5.1 Exp / Log Derivatives

2.5 Implicit Differentiation

4.4-4.5 Polynomial Integrals

5.2, 5.4 Exp / Log Integrals

5.7 Inverse Trig Derivatives

5.8 " Integrals

8.1 Basic Trig Integrals

5.8 Cont'd

Ex: Find $\int \frac{2x+8}{x^2+2x+10} dx$

$$\begin{aligned} & x^2 + 2x + 10 \\ &= x^2 + 2x + 1 + 9 \\ &= (x+1)^2 + 3^2 \end{aligned}$$

$$= \int \frac{2x+8}{(x+1)^2 + 3^2} dx$$

$u = x+1$
 $du = dx$
 $2x+8 = ?$
 $2(x+1) + 6 = ?(x+1) + ?$
 $= 2(x+1) + 6$
 $= 2u + 6$

$$= \int \frac{2u+6}{3^2 + u^2} du$$

$$= \int \left[\frac{2u}{3^2 + u^2} + \frac{6}{3^2 + u^2} \right] du$$

$$= \ln |3^2 + u^2| + \frac{6}{3} \tan^{-1} \frac{u}{3} + C$$

$$= \ln |3^2 + (x+1)^2| + 2 \tan^{-1} \frac{x+1}{3} + C$$

5.8 #17

$$\int \frac{1}{\sqrt{5} \sqrt{1-x}} dx$$

$$= \int \frac{1}{\sqrt{x} \sqrt{1-x^2}} dx$$

$$u = \sqrt{x}$$

$$du = \frac{1}{2} x^{-1/2} dx$$

$$2du = \frac{dx}{\sqrt{x}}$$

$$= 2 \int \frac{du}{\sqrt{1-u^2}}$$

$$= 2 \sin^{-1} u + C$$

$$= 2 \sin^{-1} \sqrt{x} + C$$

5.9 Won't Be Tested
Hyperbolic Functions

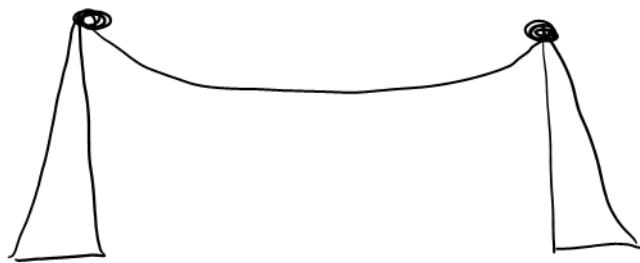
Hyperbolic Cosine

$$\cosh x = \frac{e^x + e^{-x}}{2}$$

Hyperbolic Sine

$$\sinh x = \frac{e^x - e^{-x}}{2}$$

Quick Ex: Hanging cable



$$y = a \cosh\left(\frac{x}{a}\right), \quad a > 0$$

The shape is called a catenary.

$(\cosh t, \sinh t)$ lies on
the hyperbola $x^2 - y^2 = 1$.

Hence the name

"hyperbolic functions."

$$\frac{d}{dx} [\cosh x] = \sinh x$$

$$\frac{d}{dx} [\sinh x] = \cosh x$$

$$\int \cosh x \, dx = \sinh x + C$$

$$\int \sinh x \, dx = \cosh x + C$$

Ex: Find y'

a) $y = \sinh x^3$

$$y' = 3x^2 \cosh x^3$$

b) $y = x^2 \cosh 5x$

$$y' = x^2 [\sinh 5x (5)] + (\cosh 5x)(2x)$$

$$= 5x^2 \sinh 5x + 2x \cosh 5x$$

Ex:

a) $\int \cosh 4x \, dx$

$$= \frac{1}{4} \int \cosh u \, du$$

$$= \frac{1}{4} \sinh u + C$$

$$= \frac{1}{4} \sinh 4x + C$$

$$\boxed{\begin{aligned} u &= 4x \\ du &= 4dx \\ \frac{du}{4} &= dx \end{aligned}}$$

$$b) \int x^6 \sinh x^7 dx$$

$$\begin{aligned} u &= x^7 \\ du &= 7x^6 dx \\ \frac{du}{7} &= x^6 dx \end{aligned}$$

$$= \frac{1}{7} \int \sinh u du$$

$$= \frac{1}{7} \cosh u + C$$

$$= \frac{1}{7} \cosh x^7 + C$$

8.1 Basic Trig Integrals

$$\int \sin x dx = -\cos x + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \tan x dx = \ln |\sec x| + C$$

$$\int \sec x dx = \ln |\sec x + \tan x| + C$$

$$\int \cot x dx = -\ln |\csc x| + C$$

$$\int \csc x dx = -\ln |\csc x + \cot x| + C$$

$$\int \sec^2 x dx = \tan x + C$$

$$\int \sec x \tan x dx = \sec x + C$$

$$\int \csc x \cot x dx = -\csc x + C$$

$$\int \csc^2 x dx = -\cot x + C$$