

Stat 254 Assignment One

Name: \_\_\_\_\_

**Assignments must be completed on this paper. Marks may be deducted for not showing all your work.**

1. [3 marks] The data set below represents house prices in a certain city.

Price (\$)	Relative Frequency
400,000	0.1
600,000	0.45
800,000	0.25
1,000,000	0.15
1,200,000	0.05

- a) Calculate the mean and the median.

- b) Based on the mean and the median, in which direction is the data skewed?

2. [4 marks] A data set has 1200 measurements, a mean of 65, and a standard deviation of 7. What can you say about the number of measurements that are less than 37?

3. [2 marks] Construct a data set with two measurements which has a mean of 83 and a population variance of 16. Show your work.

4. [3 marks] If the data has a linear relationship, find the equation of the least squares regression line. Round your values to one decimal place. If the data does not have a linear relationship, write *nonlinear*.

a) 
$$\begin{array}{c|cccccc} x & 1.1 & 1.6 & 0.8 & 0.7 & 1.9 & 1.2 \\ \hline y & -2.5 & -2.7 & -5.6 & -5.1 & -2.2 & -4.9 \end{array}$$

b) 
$$\begin{array}{c|cccccc} x & 3.4 & 3.7 & 2.9 & 2.6 & 2.7 & 2.2 \\ \hline y & 8.2 & 8.5 & 7.5 & 5.1 & 8.3 & 7.1 \end{array}$$

5. [4 marks] A lab has two smoke alarms. 98.8% of fires are detected by Alarm A; 98.4% of fires are detected by Alarm B; 0.7% of fires are detected by Alarm A but not Alarm B. Find the probability that a fire is detected by:

a) both alarms

b) at least one alarm

c) neither alarm

6. [3 marks] A coin is tossed eight times. Find the probability that the first three tosses are heads or the last toss is tails. Round your answer to two decimal places.

7. [3 marks] Ten percent of all cars are red. Of the red cars, 1.5% are convertibles. Of the non-red cars, 1.8% are convertibles. Find:

a) The probability that a red car is not a convertible

b) The probability that a convertible is not red

8. [3 marks] 12 deep-water and 18 shallow-water samples are drawn from the inner harbour. Four samples are randomly selected for further testing. Let  $X$  be the number of deep-water samples selected.

a) Find the probability distribution of  $X$ . Round the probabilities to two decimal places.

b) Find the expected value of  $X$