

(15)

$$\begin{aligned} \text{Total} &= 168912 + 34068 + 1020 \\ &= 204000 \end{aligned}$$

| Outcome     | Probability             |
|-------------|-------------------------|
| Public      | $\frac{168912}{204000}$ |
| Private     | $\frac{34068}{204000}$  |
| Home school | $\frac{1020}{204000}$   |

(19)

$$\begin{aligned} \text{a) } Pr(E) &= Pr(s_1) + Pr(s_2) \\ &= 0.1 + 0.6 \\ &= 0.7 \end{aligned}$$

$$\begin{aligned} Pr(F) &= Pr(s_2) + Pr(s_4) \\ &= 0.6 + 0.1 \\ &= 0.7 \end{aligned}$$

$$\begin{aligned} \text{b) } Pr(E') &= 1 - Pr(E) \\ &= 1 - 0.7 \\ &= 0.3 \end{aligned}$$

$$\begin{aligned} \text{c) } E \cap F &= \{s_2\} \\ Pr(E \cap F) &= Pr(s_2) \\ &= 0.6 \end{aligned}$$

$$\begin{aligned} \text{d) } E \cup F &= \{s_1, s_2, s_4\} \\ Pr(E \cup F) &= Pr(s_1) + Pr(s_2) + Pr(s_4) \\ &= 0.1 + 0.6 + 0.1 \\ &= 0.8 \end{aligned}$$

(25)

Let  $A$ : Horse A wins

"  $B$ : "  $B$  "

"  $C$ : "  $C$  "

$$Pr(A) + Pr(B) + Pr(C) = 1$$

$$\frac{1}{3} + \frac{1}{2} + Pr(C) = 1$$

Multiply by 6:  $2 + 3 + 6 Pr(C) = 6$

$$6 Pr(C) = 1$$

$$Pr(C) = \frac{1}{6}$$

(27)

Let  $L$ : liberal views

"  $M$ : middle-of-the-road views

"  $C$ : conservative views

$$\text{Let } \Pr(C) = x$$

$$\text{Then } \Pr(M) = 2x$$

$$\text{Given } \Pr(L) = 0.28$$

$$\Pr(L) + \Pr(M) + \Pr(C) = 1$$

$$0.28 + 2x + x = 1$$

$$3x = 0.72$$

$$x = 0.24$$

$$\Pr(C) = 0.24$$

We weren't asked for the probability distribution but it would be:

| Outcome | Probability          |
|---------|----------------------|
| L       | 0.28                 |
| M       | 0.48 $\leftarrow 2x$ |
| C       | 0.24 $\leftarrow x$  |

(31)

$E$  and  $F$  are mutually exclusive means  $E$  and  $F$  can't happen at the same time, so  $\Pr(E \cap F) = 0$   
(See Section 4.1 for more details)

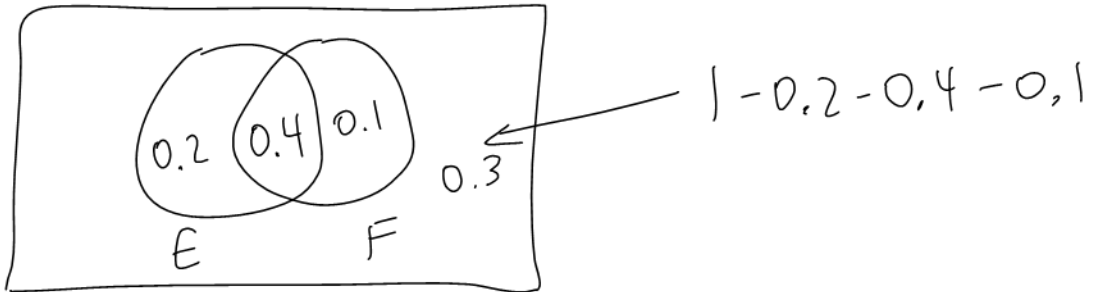
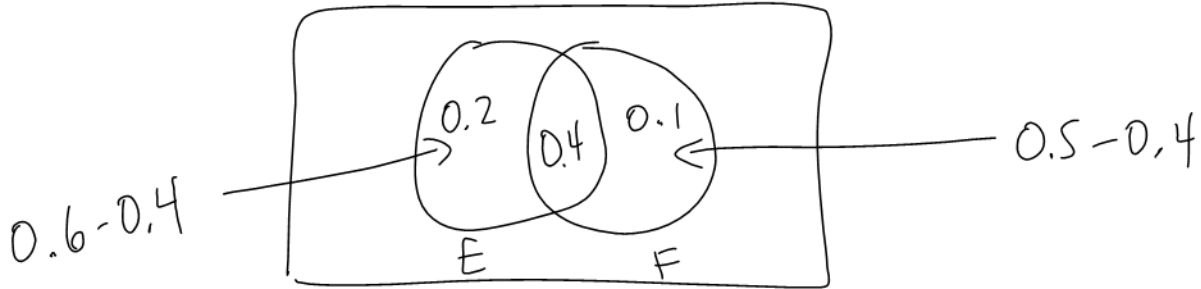
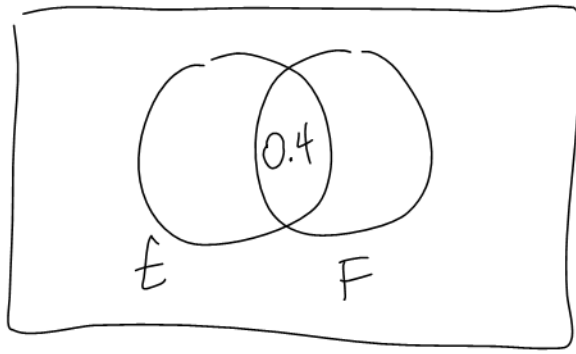
Inclusion - Exclusion Principle

$$\Pr(E \cup F) = \Pr(E) + \Pr(F) - \Pr(E \cap F)$$

$$\Pr(E \cup F) = 0.4 + 0.5 - 0$$

$$\Pr(E \cup F) = 0.9$$

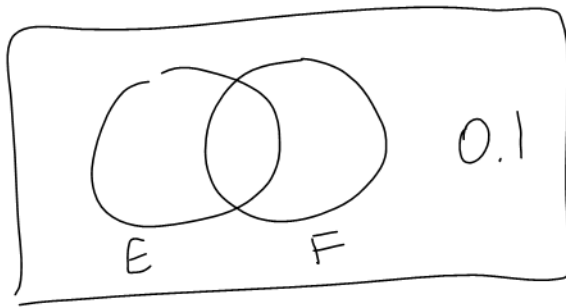
(33)



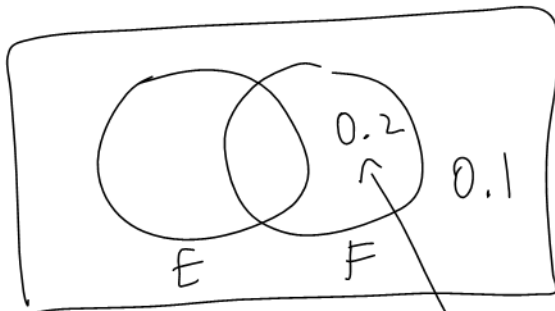
$$\begin{aligned} \text{a) } \Pr(E \cup F) &= 0.2 + 0.4 + 0.1 \\ &= 0.7 \end{aligned}$$

$$\begin{aligned} \text{b) } \Pr(\underbrace{E \cap F'}_{\substack{\text{in } E \\ \text{and not in } F}}) &= 0.2 \end{aligned}$$

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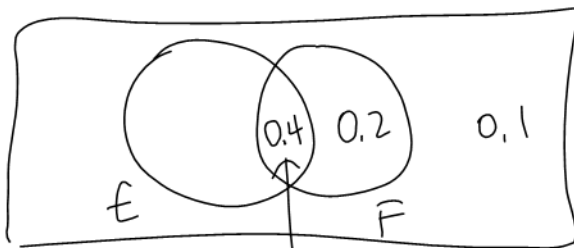


Given  $\Pr(E' \cap F') = 0.1$   
not in E  
and not in F

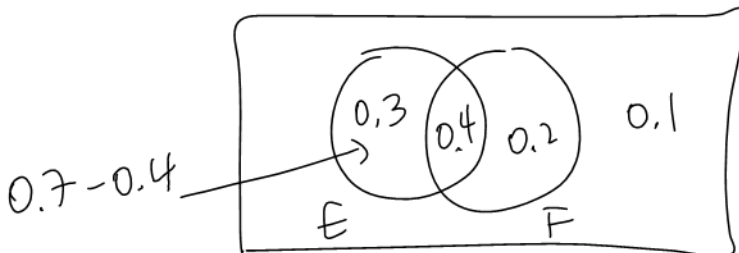


$$\begin{aligned}\Pr(E) &= 0.7 \\ \Pr(E') &= 1 - \Pr(E) \\ \Pr(E') &= 0.3\end{aligned}$$

$$0.3 - 0.1$$



$$0.6 - 0.2$$



$$\begin{aligned}a) \Pr(E \cup F) &= 0.3 + 0.4 + 0.2 = 0.9 \\ b) \Pr(E \cap F) &= 0.4\end{aligned}$$

(39)

10 : 1

$$\Pr(\text{event}) = \frac{10}{10+1}$$

$$\Pr(\text{event}) = \frac{10}{11}$$

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$$\Pr(\text{event}) = 0.2$$

The odds are

$$\Pr(\text{event}) : 1 - \Pr(\text{event})$$

$$0.2 : 0.8$$

$$( \times 10 ) \quad 2 : 8$$

$$( \div 2 ) \quad 1 : 4$$



(43)

$$\Pr(\text{event}) = 0.3125$$

The odds are

$$\Pr(\text{event}) : 1 - \Pr(\text{event})$$

$$0.3125 : 0.6875$$

$$(\times 10000) \quad 3125 : 6875$$

It's fine to leave it like this,  
or divide by 625 to get

$$5 : 11$$

(45)

$$2 : 9$$

$$\Pr(\text{event}) = \frac{2}{2+9}$$

$$\Pr(\text{event}) = \frac{2}{11}$$